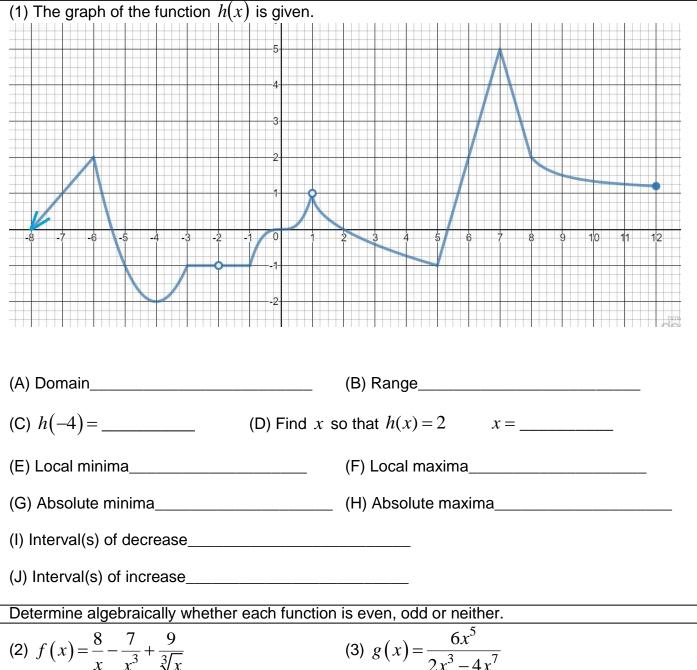
<u>AP Calculus BC</u> Summer Assignment

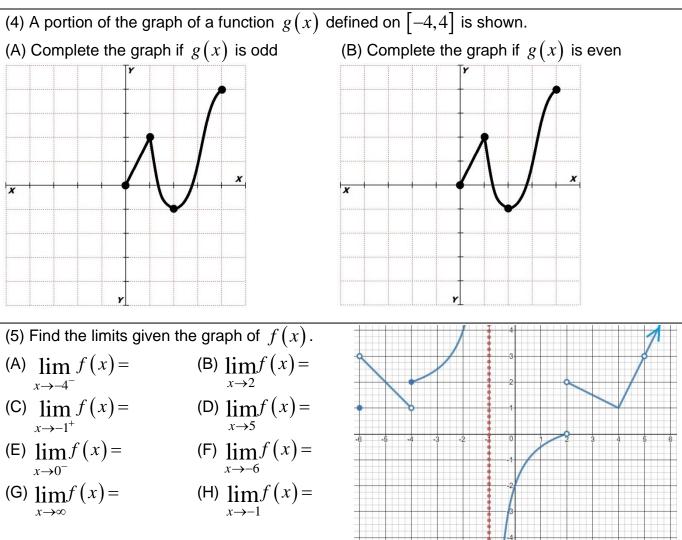
Name

Date

Show all work! Exact answers only unless the problem asks for an approximation. Determine the domain & range and evaluate each expression for the function. Then determine the value(s) of x at the local & absolute minima & maxima of the function and find the interval(s) on which the function is increasing & decreasing.

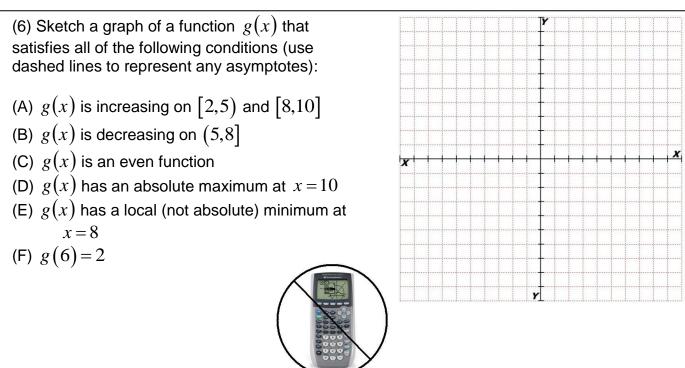






(I) At what values of x are there removable discontinuities?

(J) At what values of x are there nonremovable discontinuities?



and describe the end behavior using limits and then graph. $g(x) = -2(8x^{3} - 27)(2x^{2} + 5x - 12)(x^{2} + 8x + 16)$ End behavior model	ether the ehavior model
End behavior model $\lim_{x \to \infty} g(x) = \ \lim_{x \to -\infty} g(x) = \ x$ Identify the hole(s), vertical asymptote(s), horizontal asymptote, oblique asymptote intercept of each rational function. Then graph each rational function dashed lines for the asymptotes. Do not forget to graph the holes. Then evaluate (8) $g(x) = \frac{4x^4 - 13x^2 + 9}{x^4 + 3x^3 - 4x^2}$ Hole(s) Hole(s) Horizontal asymptote(s) Horizontal asymptote(s) Horizontal asymptote(s) Horizontal asymptote(s) Horizontal asymptote Horizontal	
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$\lim_{x \to -\infty} g(x) = \underline{\qquad} \qquad $	
$\lim_{x \to 0^+} g(x) = \underline{\qquad} \qquad \qquad \lim_{x \to 0} g(x) = \underline{\qquad}$	
$\lim_{x \to 1^{-}} g(x) = \underline{\qquad} \qquad $	
1	
$\lim_{x \to -4^+} g(x) = \underline{\qquad} \qquad $	
(9) Solve the inequality, graph the solution set & write the solution in interval nota $(r+1)^3(r^2-10r+25)$	ation.
$\frac{(x+1)^3 (x^2 - 10x + 25)}{(3x^2 + 10x - 8)(x+4)} \ge 0$	\rightarrow

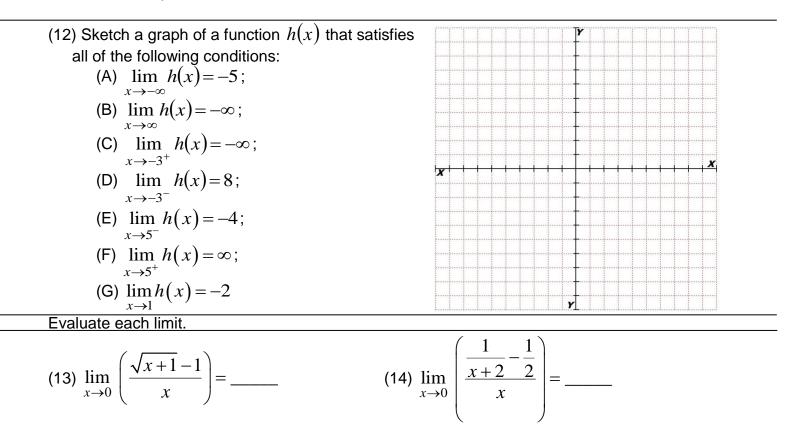
Interval Notation_____

(10) Solve the inequality, graph the solution set & write the solution in interval notation. $\frac{12}{x^2 - 16} - \frac{24}{x - 4} \le 3$

Interval Notation

(11) Determine the value of k that makes the function continuous.

$$g(x) = \begin{cases} kx^2 - 4x - 3, \ x \le -2\\ \frac{3}{2}x + 6, \ x > -2 \end{cases}$$



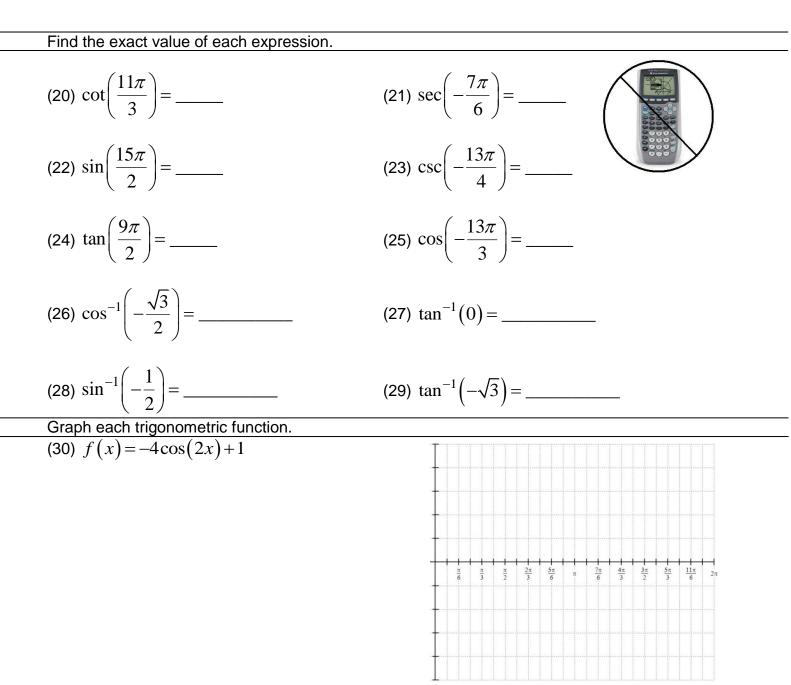
Find a formula for $f^{-1}(x) \& g^{-1}(x)$ then determine the domain and range of their inverse.

(15)
$$f(x) = -\sqrt{x-1} - 4$$
 (16) $g(x) = \frac{5-3x}{x+4}$



Solve each equation.
(17)
$$\ln(6x) - \ln(x+5) + 3\ln 4 = 2$$
 (18) $\pi^{2x+3} = e^{x-4}$

(19) Determine the logistic function $P(x) = \frac{c}{1+a \bullet b^x}$ whose initial population is 4, carrying capacity is 36 and passing through (12, 24).



5

Solve each equation on the interval $[0,2\pi)$.	
(31) $2 + 5\csc(4\theta) = -1 + 2\csc(4\theta)$	(32) $\cot\theta + \cos\theta = -2\cot\theta \cdot \cos\theta + \cos\theta$

(33)
$$3 = 3\sin\theta + 2\sin^2\theta + 4$$
 (34)

(34)
$$\sec\theta = 1 - \tan^2\theta$$

(35) Simplify the expression. $\cos\theta \bullet \cot\theta \bullet \sin\theta \bullet \sec\theta =$

(36) Simplify the expression. $\frac{\sin^2 \theta + \tan^2 \theta + \cos^2 \theta}{\sec \theta} = \underline{\qquad}$

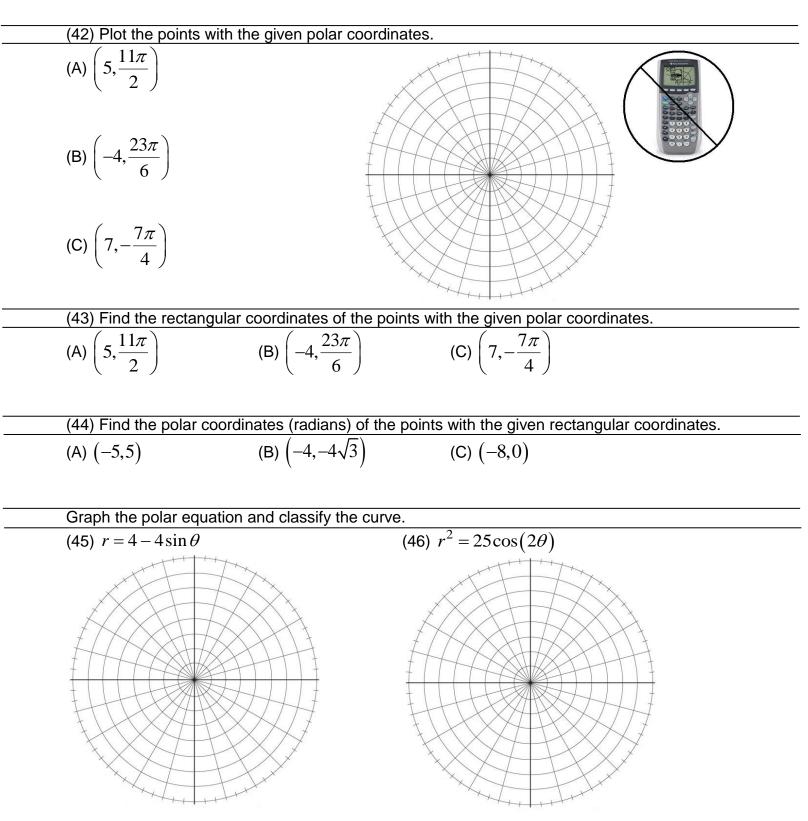
(37) Simplify the expression. $\frac{1 + \tan \theta}{\sin \theta + \cos \theta} = \underline{\qquad}$

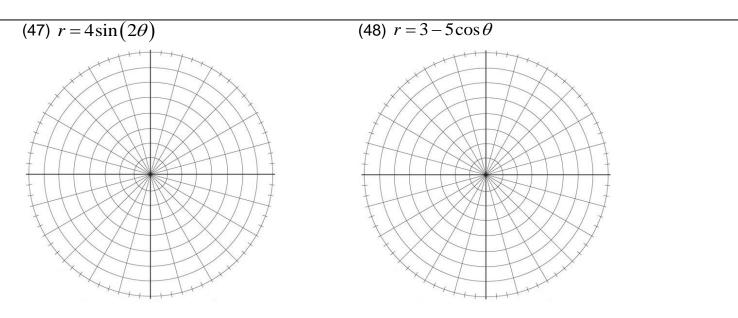
(38) Simplify the expression. $\frac{\sin\theta}{1+\cos\theta} + \frac{1+\cos\theta}{\sin\theta} = -----$

(39) Simplify the expression. $\frac{1 - \tan^2 \theta}{\tan^2 \theta + 1} + 1 = \underline{\qquad}$



Find all solutions to the equations in the interval $[0,2\pi)$.		
(40) $\sin(2\theta) \bullet \cos\theta = \sin\theta$	$(41) \cos(2\theta) = 4\cos\theta - 3$	





(49) Find the partial fraction decomposition of the rational expression. $\frac{x^2 - 19x + 17}{(x-4)(2x^2 + 3x - 1)}$



(50) Rewrite the improper rational expression as the sum of a polynomial and a proper rational expression, then find the partial fraction decomposition of the proper rational expression. Finally, express the improper rational expression as the sum of a polynomial and the partial fraction decomposition.

$$\frac{x^3 - 5x^2 + 21}{x^2 - x - 2}$$

(51) Find the average rate of change of each function over the given interval. $f(x) = -x^2 + 2x; [-1,4]$ Use the definition of the derivative to find the derivative of the each function. Then find the instantaneous rate of change of each function at the given value of x.

(52)
$$g(x) = \frac{-4}{x+2}$$



Derivative g'(x) =_____

Instantaneous rate of change at x = -3 slope = _____

(53)
$$h(x) = \sqrt{2x+7}$$

Derivative h'(x) =_____

Instantaneous rate of change at x = 1 slope =______ (54) Write the equation in standard form and classify the conic section. Identify the important characteristics of the graph.

 $x^2 + 16y^2 + 10x - 64y + 25 = 0$

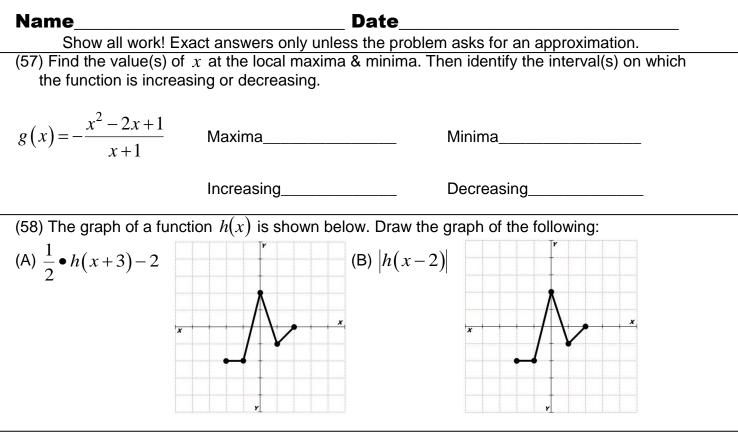
(55) Write the equation in standard form and classify the conic section. Identify the important characteristics of the graph.

$$x^2 + y^2 + 4x - 6y - 87 = 0$$

(56) Determine the values a and b that make f(x) differentiable at x = -1. Use the Definition of the Derivative or the Alternative Form.

$$f(x) = \begin{cases} \frac{2}{x-1}, \ x > -1\\ ax^2 + b, \ x \le -1 \end{cases}$$

<u>AP Calculus BC</u> Summer Assignment



- (59) MetroMedia Cable is asked to provide service to a customer whose house is located 3 miles from the road along which the cable is buried. The nearest connection box for the cable is located 7 miles down the road. If the installation cost is \$300 per mile along the road and \$450 per mile off the road, build a model that expresses the total cost of installation as a function of the distance from the connection box to the point where the cable installation turns off the road. Find the distance from the connection box that the company must turn off the road to minimize the cost. What is the minimum cost?
- (60) A company must design and build a 400 ft^3 box for a product they are putting out on the market. To accommodate the size of the product, the length needs to be 4 times longer than the width. Find dimensions that will minimize the amount of carboard that is used to make it. How much cardboard is to be used to make the box?



(61) A culture of bacteria obeys the law of uninhibited growth. If 50,000 bacteria are present initially, and there are 850,000 after 6 hours, find the exponential function $A(t) = ae^{kt}$ that models this data (round to 3 decimal places).

(62) A cup of coffee is heated to 182°F and is then allowed to cool in a room whose air temperature is 68°F. After 9 minutes, the temperature of the cup of coffee is 142°F. Find the function that represents this situation and the time needed for the coffee to cool to a temperature of 100°F (round to 3 decimal places).



(63) The number of students infected with the flu at Sunnyside High School after *t* days is modeled by the function $F(t) = \frac{900}{1+59e^{-0.138t}}$.

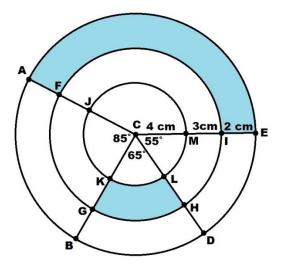
A) What was the initial number of infected students?

B) How many students will be infected after 11 days?

C) The school will close when 300 of the 900 student body are infected. When will school close (round to 3 decimal places)?

(64) Find the length of arc FI (round to 3 decimal places).

(65) Find the total area of the shaded regions (round to 3 decimal places).



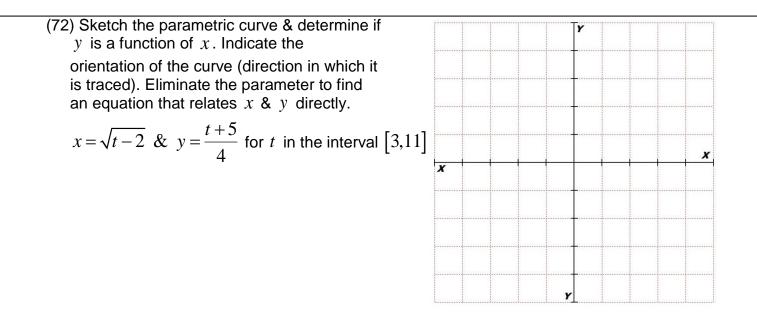
Find the sum of the series. (66) 21+25+29+33+...;n = 26

(67) 2+6+18+54+...;n=13

(68) 20480 + 5120 + 1280 + 320 + ...

(70) 29 + 22 + 15 + 8 + ... + (-160)

(71)
$$12288 + (-6144) + 3072 + ... + (-\frac{3}{2})$$



(73) An airplane, flying in the direction 20° east of north at 325 mph in still air, encounters a 40mph tail wind acting in the direction of 40° west of north. The airplane maintains its compass heading but, because of the wind, acquires a new ground speed and direction. What are they?

